

#### **Lecture PowerPoints**

Chapter 5

Physics: Principles with Applications, 6<sup>th</sup> edition

Giancoli

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## Chapter 5

## Circular Motion; Gravitation



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## **Units of Chapter 5**

- Kinematics of Uniform Circular Motion
- Dynamics of Uniform Circular Motion
- Highway Curves, Banked and Unbanked
- Nonuniform Circular Motion
- Centrifugation
- Newton's Law of Universal Gravitation

### **Units of Chapter 5**

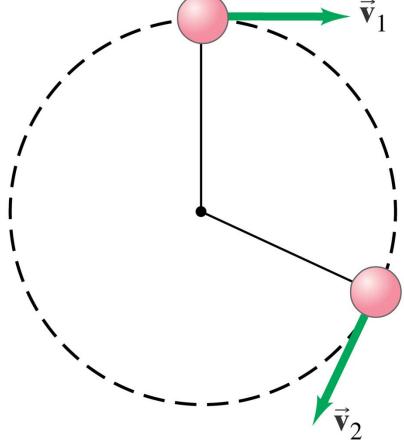
- Gravity Near the Earth's Surface; Geophysical Applications
- Satellites and "Weightlessness"
- Kepler's Laws and Newton's Synthesis
- Types of Forces in Nature

#### 5-1 Kinematics of Uniform Circular Motion

Uniform circular motion: motion in a circle of constant radius at constant speed

Instantaneous velocity is always tangent to

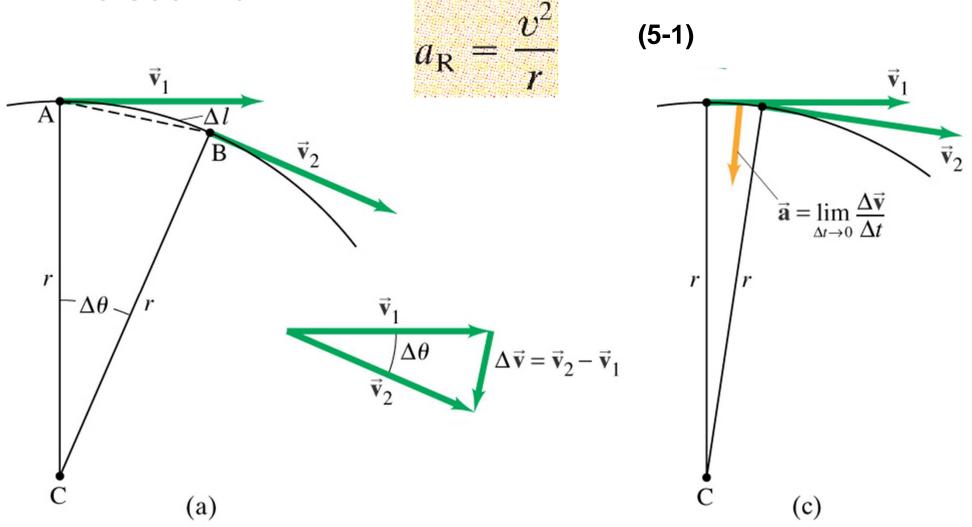
circle.



#### 5-1 Kinematics of Uniform Circular Motion

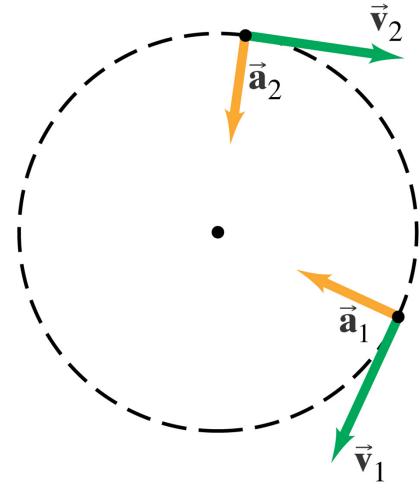
Looking at the change in velocity in the limit that the time interval becomes infinitesimally small,

we see that



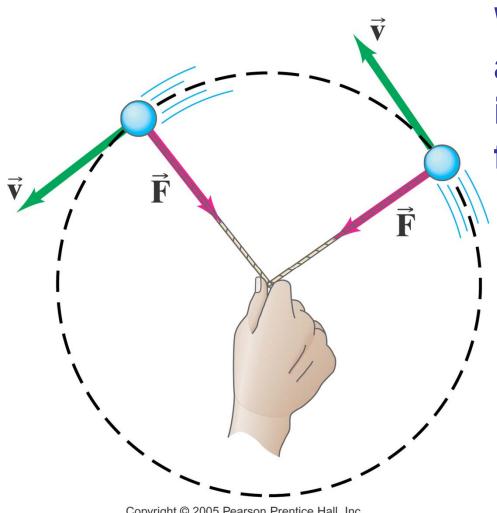
#### 5-1 Kinematics of Uniform Circular Motion

This acceleration is called the centripetal, or radial, acceleration, and it points towards the center of the circle.



## 5-2 Dynamics of Uniform Circular Motion

For an object to be in uniform circular motion, there must be a net force acting on it.

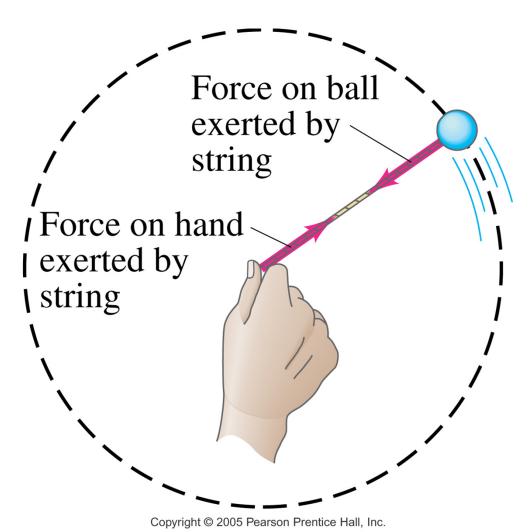


We already know the acceleration, so can immediately write the force:

$$\Sigma F_{\rm R} = ma_{\rm R} = m\frac{v^2}{r}$$
(5-1)

## 5-2 Dynamics of Uniform Circular Motion

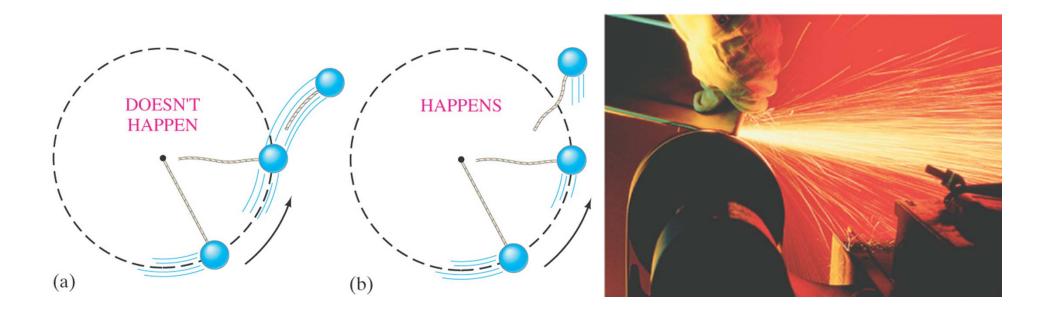
We can see that the force must be inward by thinking about a ball on a string:



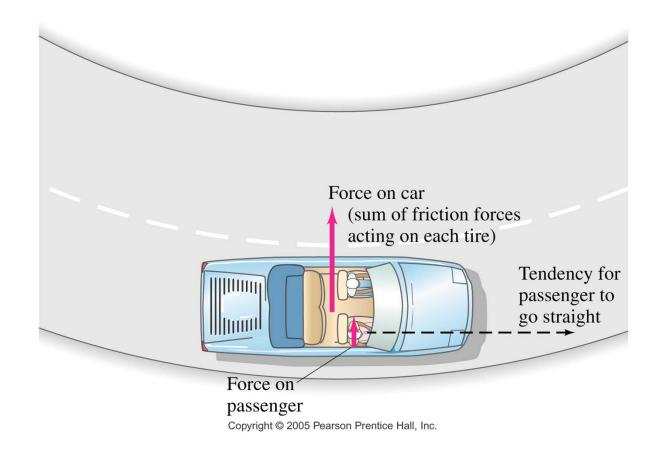
## 5-2 Dynamics of Uniform Circular Motion

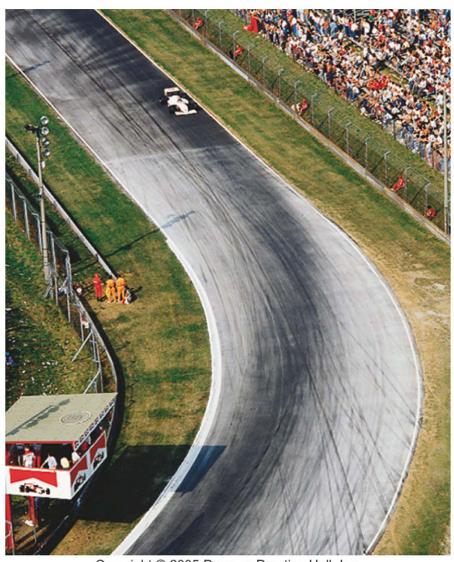
There is no centrifugal force pointing outward; what happens is that the natural tendency of the object to move in a straight line must be overcome.

If the centripetal force vanishes, the object flies off tangent to the circle.



When a car goes around a curve, there must be a net force towards the center of the circle of which the curve is an arc. If the road is flat, that force is supplied by friction.

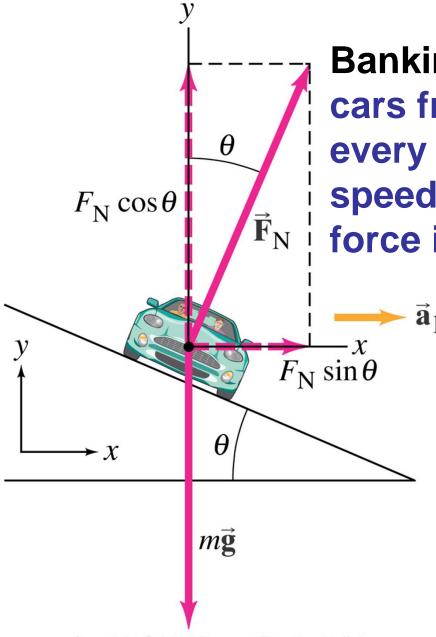




If the frictional force is insufficient, the car will tend to move more nearly in a straight line, as the skid marks show.

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- As long as the tires do not slip, the friction is static. If the tires do start to slip, the friction is kinetic, which is bad in two ways:
- 1. The kinetic frictional force is smaller than the static.
- 2. The static frictional force can point towards the center of the circle, but the kinetic frictional force opposes the direction of motion, making it very difficult to regain control of the car and continue around the curve.

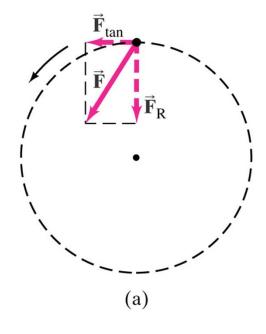


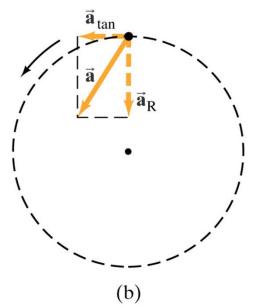
Banking the curve can help keep cars from skidding. In fact, for every banked curve, there is one speed where the entire centripetal force is supplied by the

horizontal component of  $\vec{a}_R$  the normal force, and no friction is required. This occurs when:

$$F_{\rm N}\sin\theta = m\frac{v^2}{r}$$

#### 5-4 Nonuniform Circular Motion

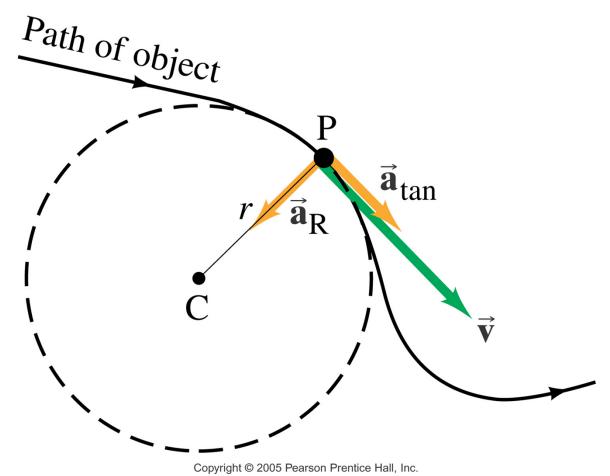




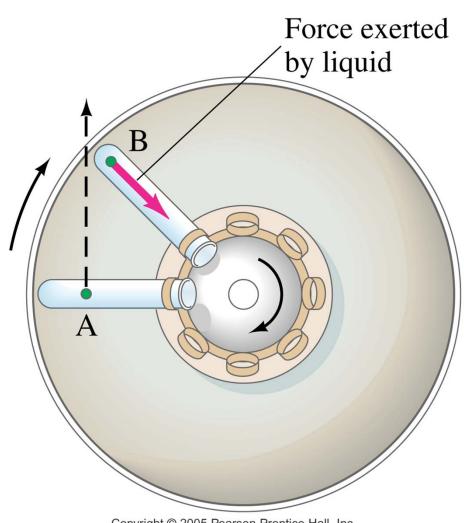
If an object is moving in a circular path but at varying speeds, it must have a tangential component to its acceleration as well as the radial one.

#### 5-4 Nonuniform Circular Motion

This concept can be used for an object moving along any curved path, as a small segment of the path will be approximately circular.



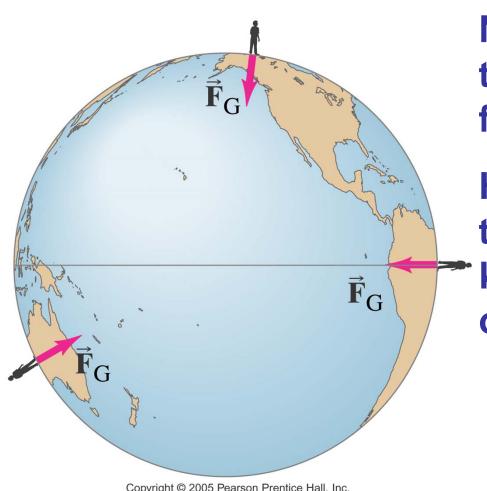
## 5-5 Centrifugation



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A centrifuge works by spinning very fast. This means there must be a very large centripetal force. The object at A would go in a straight line but for this force; as it is, it winds up at B.

If the force of gravity is being exerted on objects on Earth, what is the origin of that force?

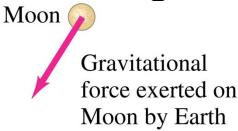


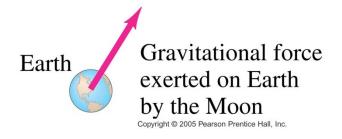
**Newton's realization was** that the force must come from the Earth.

He further realized that this force must be what keeps the Moon in its orbit.

The gravitational force on you is one-half of a Third Law pair: the Earth exerts a downward force on you, and you exert an upward force on the Earth.

When there is such a disparity in masses, the reaction force is undetectable, but for bodies more equal in mass it can be significant.





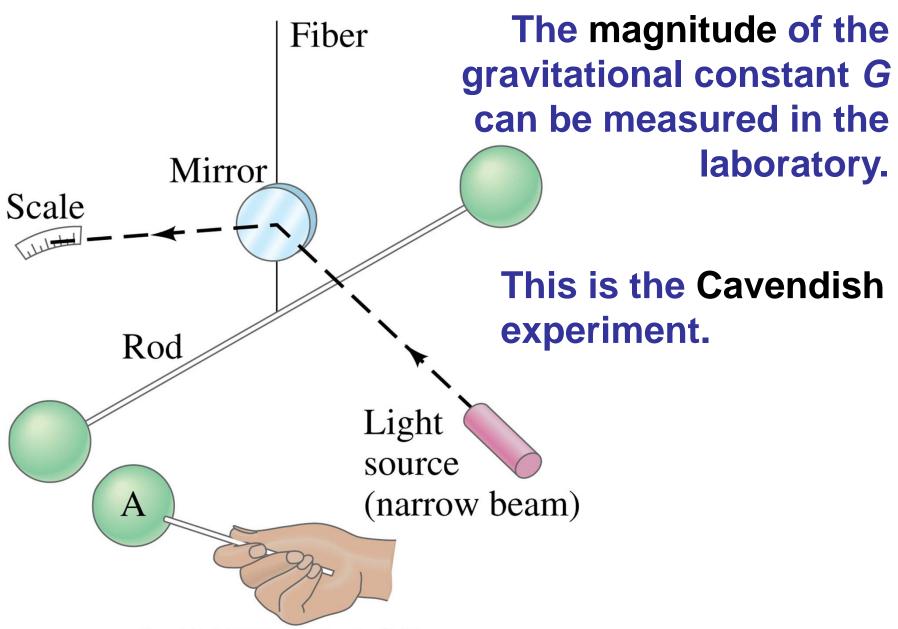
Therefore, the gravitational force must be proportional to both masses.

By observing planetary orbits, Newton also concluded that the gravitational force must decrease as the inverse of the square of the distance between the masses.

In its final form, the Law of Universal Gravitation reads:  $m_1 m_2$ 

Pads: 
$$F = G \frac{m_1 m_2}{r^2}$$
 (5-4)

where 
$$G = 6.67 \times 10^{-11} \,\text{N} \cdot \text{m}^2/\text{kg}^2$$



## 5-7 Gravity Near the Earth's Surface; **Geophysical Applications**

Now we can relate the gravitational constant to the local acceleration of gravity. We know that, on the surface of the Earth:  $mg = G \frac{mm_{\rm E}}{r_{\rm E}^2}$ 

$$mg = G \frac{mm_{\rm E}}{r_{\rm E}^2}$$

Solving for g gives:  $g = G \frac{m_E}{r_E^2}$ 

$$g = G \frac{m_{\rm E}}{r_{\rm E}^2} \tag{5-5}$$

Now, knowing g and the radius of the Earth, the mass of the Earth can be calculated:

$$m_{\rm E} = \frac{gr_{\rm E}^2}{G} = \frac{(9.80 \,\mathrm{m/s^2})(6.38 \times 10^6 \,\mathrm{m})^2}{6.67 \times 10^{-11} \,\mathrm{N \cdot m^2/kg^2}} = 5.98 \times 10^{24}$$

# 5-7 Gravity Near the Earth's Surface; Geophysical Applications

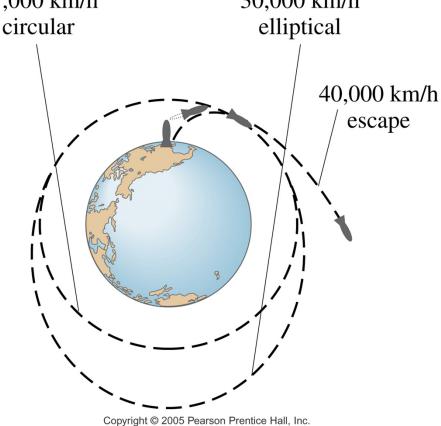
# TABLE 5–1 Acceleration Due to Gravity at Various Locations on Earth

Location	Elevation (m)	g (m/s <sup>2</sup> )
New York	0	9.803
San Francisco	0	9.800
Denver	1650	9.796
Pikes Peak	4300	9.789
Sydney, Australia	0	9.798
Equator	0	9.780
North Pole (calculated)	0	9.832

The acceleration due to gravity varies over the Earth's surface due to altitude, local geology, and the shape of the Earth, which is not quite spherical.

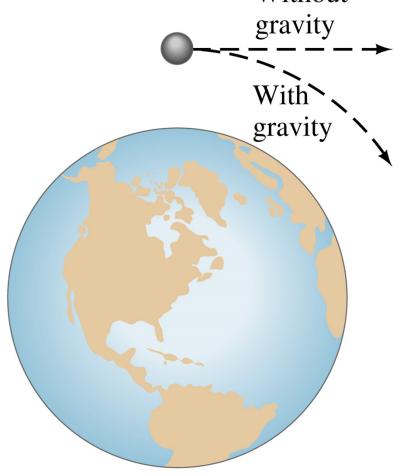
Satellites are routinely put into orbit around the Earth. The tangential speed must be high enough so that the satellite does not return to Earth, but not so high that it escapes Earth's gravity altogether.

27,000 km/h
30,000 km/h



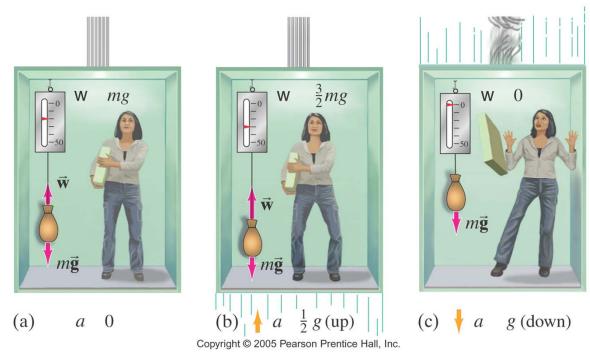
The satellite is kept in orbit by its speed – it is continually falling, but the Earth curves from underneath it.

Without



Objects in orbit are said to experience weightlessness. They do have a gravitational force acting on them, though!

The satellite and all its contents are in free fall, so there is no normal force. This is what leads to the experience of weightlessness.

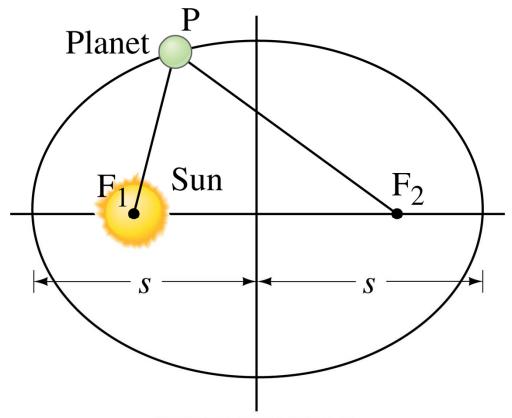


More properly, this effect is called apparent weightlessness, because the gravitational force still exists. It can be experienced on Earth as well, but only briefly:

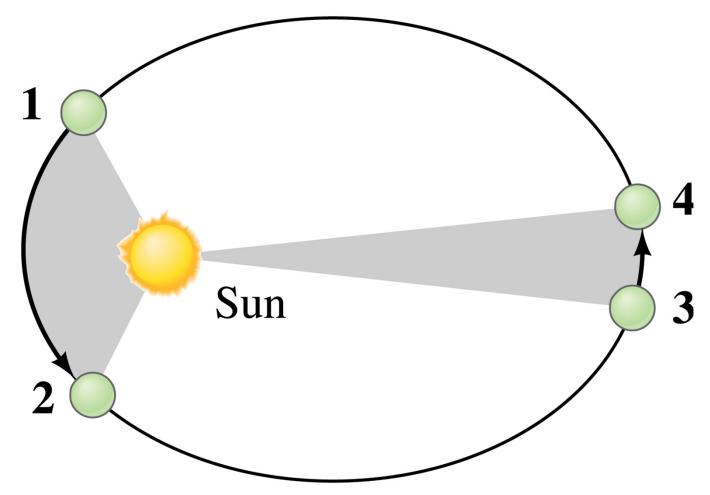


Kepler's laws describe planetary motion.

1. The orbit of each planet is an ellipse, with the Sun at one focus.



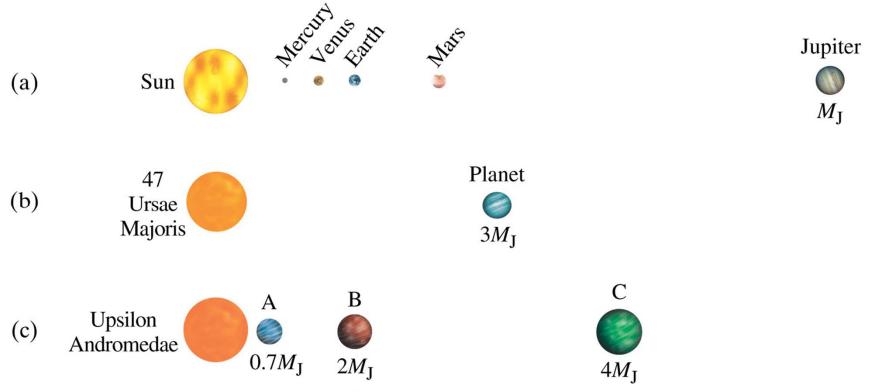
2. An imaginary line drawn from each planet to the Sun sweeps out equal areas in equal times.



The ratio of the square of a planet's orbital period is proportional to the cube of its mean distance from the Sun.

TABLE 5-2 Planetary Data Applied to Kepler's Third Law				
Planet	Mean Distance from Sun, <i>s</i> (10 <sup>6</sup> km)	Period, T (Earth years)	$s^3/T^2$ (10 <sup>24</sup> km <sup>3</sup> /y <sup>2</sup> )	
Mercury	57.9	0.241	3.34	
Venus	108.2	0.615	3.35	
Earth	149.6	1.0	3.35	
Mars	227.9	1.88	3.35	
Jupiter	778.3	11.86	3.35	
Saturn	1427	29.5	3.34	
Uranus	2870	84.0	3.35	
Neptune	4497	165	3.34	
Pluto	5900	248	3.34	

Kepler's laws can be derived from Newton's laws. Irregularities in planetary motion led to the discovery of Neptune, and irregularities in stellar motion have led to the discovery of many planets outside our Solar System.



## 5-10 Types of Forces in Nature

Modern physics now recognizes four fundamental forces:

- 1. Gravity
- 2. Electromagnetism
- 3. Weak nuclear force (responsible for some types of radioactive decay)
- 4. Strong nuclear force (binds protons and neutrons together in the nucleus)

## 5-10 Types of Forces in Nature

So, what about friction, the normal force, tension, and so on?

Except for gravity, the forces we experience every day are due to electromagnetic forces acting at the atomic level.

## **Summary of Chapter 5**

- An object moving in a circle at constant speed is in uniform circular motion.
- It has a centripetal acceleration  $a_{\rm R} = \frac{v^2}{r}$
- There is a centripetal force given by

$$\Sigma F_{\rm R} = ma_{\rm R} = m\frac{v^2}{r}$$

•The centripetal force may be provided by friction, gravity, tension, the normal force, or others.

## **Summary of Chapter 5**

Newton's law of universal gravitation:

$$F = G \frac{m_1 m_2}{r^2}$$

•Satellites are able to stay in Earth orbit because of their large tangential speed.